Searching for L-violating supersymmetry at the LHC

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Abstract. The possibility to simulate lepton number violating supersymmetric models has been introduced into the recently updated Pythia event generator, now containing 1278 decay channels of SUSY particles into SM particles via lepton number violating interactions. This generator has been used in combination with the AtlFast detector simulation to study the impact of lepton number violation ($\not\!\!L$) on event topologies in the ATLAS detector, and trigger menus designed for $\not\!\!L$ -SUSY are proposed based on very general considerations. In addition, a rather preliminary analysis is presented on the possibility for ATLAS to observe a signal above the background in several mSUGRA scenarios, using a combination of primitive cuts and neural networks to optimize the discriminating power between signal and background events over regions of parameter space rather than at individual points. It is found that a 5σ discovery is possible roughly for $m_{1/2} < 1\,\text{TeV}$ and $m_0 < 2\,\text{TeV}$ with an integrated luminosity of $30\,\text{fb}^{-1}$, corresponding to one year of data taking with the LHC running at "mid-luminosity", $\mathcal{L} = 3 \times 10^{33}\,\text{cm}^{-2}\text{s}^{-1}$.

1 Introduction

Among the primary physics goals of the Large Hadron Collider at CERN, scheduled to turn on some time during 2006, are the exploration of the SM Higgs and top quark sectors, and the direct exploration of the TeV scale with the emphasis on supersymmetry.

The motivations for believing that supersymmetry is indeed a property of nature are many, most importantly the natural and exhaustive extension of the Poincaré group furnished by the supersymmetric operators [1], the possibility for exact unification of the SM gauge couplings as required by GUTs, the requirement of supersymmetry for anomaly cancellation in string theories, and perhaps most importantly, its providing a natural and elegant solution to the problem of scale hierarchy in the SM.

For this latter problem to be solved without unnatural finetuning order by order in perturbation theory, the sparticle masses must lie at or below the TeV scale, and so there is ample reason to believe that SUSY should be observable at the LHC (see e.g. [2]).

The potential for hadron colliders to observe supersymmetry has been studied in great detail (see e.g. [3, 4]), yet studies tend to concentrate on the simple MSSM framework where both baryon and lepton number conservation are imposed. In Sect. 2 we summarize the theoretical situation, pointing out that it is by no means obvious that baryon and lepton number should be conserved in supersymmetric theories. The possibility to study lepton and baryon number violating supersymmetry has already been included [5] in the Herwig event generator [6] and in SusyGen [7], and several studies exist for run II of the Tevatron (for reviews, see [8,9], and for the latest experimental results [10]) and to a lesser extent for the LHC (see e.g. [11–14]).

However, it has not before been possible to study the full range of decays in these supersymmetric models using the Pythia framework (and thus the string fragmentation model), and no dedicated LHC studies have been performed regarding triggers and sensitivity for these theories beyond cases where the LSP was simply forced to decay. In this paper, we go to the general case where all sparticles (excepting the gluino) are allowed to decay via lepton number violating couplings, introducing 1278 lepton number violating decay channels of sparticles to particles in the Pythia event generator.

For the purpose of studying the experimental signatures arising from the lepton number violating decay channels, and to quantify to some extent the "discovery potential" of the LHC, some selection of benchmark points is needed. 5 mSUGRA points and, for each of these, 9 scenarios for the 36 $\rlap/$ $\rlap/$ coupling strengths are presented and discussed in Sect. 3.

From this point on, the analysis relies on technical aspects of the detector design (or rather, their representation in crude simulation algorithms), and so we are forced to distinguish between the ATLAS and CMS experiments. Assuming to a first approximation that these experiments will have similar capabilities, we choose to concentrate on ATLAS in the remainder of the paper.

A first step is to define the data sample inside which \mathbb{Z} -SUSY should be searched for. To this purpose, a selec-

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tion of triggers designed for L-SUSY scenarios are proposed for "mid-luminosity" running of the LHC ($\mathcal{L} = 3 \times 10^{33} \, \mathrm{cm}^{-2} \mathrm{s}^{-1}$) in Sect. 4.

Before going further, we note that the conventional procedure of studying a few benchmark points in detail is insufficient in the enlarged parameter space opened up by the *L*-violating couplings, even more so since the presence of such couplings also remove important cosmological contraints on the mSUGRA parameters. In particular, the lightest supersymmetric particle (LSP) is no longer required to be neutral [15], and essentially no bound on the mSUGRA parameters can be obtained by requiring a relic density less than or equal to the density of dark matter in the universe.

In Sect. 5, we make a first attempt to come to grips with the size of the parameter space, proposing a method which relies on neural networks and the grouping of individual scenarios into classes, whereby regions rather than individual points become the studied objects in parameter space. In this work, we define just 2 classes of $I\!\!L$ -SUSY models, each containing 15 individual scenarios and a class consisting of 5 MSSM scenarios for reference. For each class, a neural network is trained with post-trigger events from all the scenarios in the class against background events, allowing the network to pick out general qualities common to each class without over-fitting to a particular model. Although we study only a few scenarios here, the usefulness of this method should become apparent when considering the requirements posed by more comprehensive scans over parameter space.

After some remarks pertaining to the dangers of using neural networks, we present results for the estimated ATLAS sensitivity, $S/(S+B)^{1/2}$, for all scenarios with an assumed integrated luminosity of 30 fb^{-1} . The subsequent step of pinning down the model parameters once a signal has been observed, is clearly more model dependent and is not covered here. An up-to-date review can be found in [9].

A brief outlook and concluding remarks are given in Sect. 6.

2 *L*-violating SUSY

In this part of the paper, we do not present new results. Rather, we summarize some theoretical considerations concerning R-violation which, although well documented in the literature, may not be in the active memory of all readers.

Despite the many attractive features of supersymmetry, most notably that it provides a natural solution to the hierarchy problem, it is well known that the most general supersymmetric Lagrangian (containing all terms obeying $SU(3)_C \times SU(2)_L \times U(1)_Y$ gauge invariance and supersymmetry) is utterly incompatible with experiment, regardless of whether the assumption of minimal particle content is made or not.

The reason is that baryon and lepton number conservation is not guaranteed by any of the symmetries just

mentioned, and the accidental conservation of these quantum numbers in the SM does not hold when extending the SM with supersymmetry; the full SUSY Lagrangian contains renormalizable lepton and baryon number violating operators [16] which are suppressed only by the SUSY breaking mass scale squared. Unless a much more powerful suppression mechanism is also at work, these operators result in a lifetime for the proton which would be measured in fractions of a second, to be compared with the experimental bound $\tau_p > 1.6 \times 10^{33} \,\mathrm{yr}$ (at 90% CL) obtained by Super-Kamiokande in the $p \to e^+ \pi^0$ channel [17].

The possibility that the couplings responsible for proton decay are just naturally small but not zero is almost out of the question. Assuming $M_{\rm SUSY}\approx 1\,{\rm TeV}$, the product of the $\not\!\!\!B$ and $\not\!\!\!\!L$ couplings involved in proton decay is required to be less than 10^{-25} [18]. Since at least one of the couplings is then forced to have a value below 10^{-12} without any obvious suppression mechanism at work, it is more natural to assume that there is some additional symmetry in the theory, giving zero couplings either for the B-violating terms, the L-violating terms, or both.

Thus, in the minimal supersymmetric standard model (MSSM), a discrete symmetry, R-parity [19], is customarily imposed which ensures the conservation of baryon as well as lepton number in the supersymmetric Lagrangian. Since there are strong indications that non-gauged symmetries are maximally violated by quantum gravity effects (leading to wormhole-induced proton decay [20]) whereas gauged symmetries are totally stable against such effects [21], we shall here assume that the proton-protecting symmetry is in fact a so-called discrete gauge symmetry [22]. In this case, it is of importance to note that although Rparity conservation leads to a comparatively simple phenomenology and a natural dark matter candidate (the LSP), the problem with proton decay is not satisfactorily solved when embedding the supersymmetric theory into more fundamental frameworks (such as GUTs) where baryon and lepton number violation can appear at some higher scale.

In an effective theory valid around the electroweak energy scale, the interactions mediated by super-heavy resonances associated with a higher-scale theory, take the form of non-renormalizable operators (i.e. operators of mass dimension $d \geq 5$) suppressed by d-4 powers of the high scale. Such operators, violating baryon and/or lepton number are generally not forbidden by R-parity conservation (see Fig. 1), and it has been demonstrated that operators of dimension 5, being suppressed by only one power of the high (e.g. GUT) scale, will cause too rapid proton decay unless their couplings are suppressed by several orders of magnitude [23]. This should, by itself, provide a powerful argument for exploring alternatives to R-parity.

In [24], a systematic analysis of discrete gauge symmetries was carried out with the surprising conclusion that only R-parity and a Z_3 symmetry equivalent to L-conservation are anomaly-free, although some model dependence of this analysis [25] implies that also conservation of baryon number could be assured by viable sym-

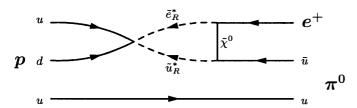


Fig. 1. An example of proton decay proceeding via a 5-dimensional operator violating both L and B but conserving R. Due to the Majorana nature of the neutralino, it is drawn without an arrow

metries. We shall here denote the two possibilities by L-parity and B-parity, though this should not be taken to mean that these symmetries stand for exact lepton number conservation and exact baryon number conservation (for obvious reasons to do with the matter—antimatter asymmetry of the universe). These names only reflect that in the supersymmetric part of the theory, the corresponding quantities are conserved. They may still be violated by GUT scale operators and will certainly be so by electroweak sphalerons. By far the most interesting observation, however, is that both L-parity and B-parity but not R-parity can forbid the dangerous dimension 5 contributions to proton decay.

Since a large number of current GUT and Planck scale theories do contain baryon and lepton number violation exterior to the supersymmetric MSSM framework, which will result in exactly this kind of contributions, it is important that experiments planning to explore SUSY are well prepared for the very distinct experimental signatures which are the hallmarks of *R*-parity violating scenarios, most importantly the consequences of a decaying LSP, of single sparticle production, and of the removal of the cosmological constraint that the LSP be neutral.

In this article, we assume the framework of the MSSM with the modification that lepton number is violated. This leads to the MSSM interaction Lagrangian being enlarged by the following terms [18]:

$$\mathcal{L}_{I\!\!\!/} = \lambda_{ijk} \left(\bar{\nu}_{Li}^c e_{Lj} \tilde{e}_{Rk}^* + \nu_{Li} \tilde{e}_{Lj} \bar{e}_{Rk} + \tilde{\nu}_{Li} e_{Lj} \bar{e}_{Rk} - i \leftrightarrow j \right)
+ \lambda'_{ijk} \left(\bar{\nu}_{Li}^c d_{Lj} \tilde{d}_{Rk}^* + \nu_{Li} \tilde{d}_{Lj} \bar{d}_{Rk} + \tilde{\nu}_{Li} d_{Lj} \bar{d}_{Rk} \right)
- \bar{e}_{Ri}^c u_{Lj} \tilde{d}_{Rk}^* - e_{Li} \tilde{u}_{Lj} \bar{d}_{Rk} - \tilde{e}_{Li} u_{Lj} \bar{d}_{Rk} \right)
+ h.c.,$$
(1)

where i, j, k are generation indices (summation implied) and λ_{ijk} is antisymmetric in its first two indices. The terms in the first line of the above equation are customarily denoted LLE terms and the terms in the second one LQD, in reference to the superfields appearing in the superpotential from which (1) is derived. All of these terms contain two (SM) fermions and one (SUSY) scalar. The oddness under R is thus directly visible here, since the SM fields have R=+1 and the SUSY fields R=-1. Also, it is clear that each sfermion can decay in a number of ways to two SM fermions via these couplings. L-violating neutralino, chargino, and gluino decays are forced to proceed via one or more intermediate scalar resonances.

A complete list of decay modes and full matrix elements for all decays of MSSM sparticles to SM particles can be found in [26]. Of these, we have implemented all but the gluino decays into the Pythia event generator, publicly available from version 6.2, with documentation included in the recently revised Pythia manual [27]. The conclusions of the present paper are not expected to be changed significantly by the inclusion of $\not\!\!L$ gluino decays since the gluino is typically heavy and thus has a number of other, unsuppressed decay channels available. Details of the Pythia implementation can be found in [28].

Note that the sfermion decay matrix elements in [26] have been checked analytically by the author, and that the matrix elements listed there are not directly applicable in Pythia. Both Pythia and Herwig (Isawig) follow [29,30] for the chargino and neutralino mixing conventions, but Herwig uses the opposite convention [31] for the sfermion mixing angles, yielding a relative transposition between the two programs. In addition, extensive counter-checks were made between the two programs to make sure they agree¹. Some non-negligible differences exist:

- (1) Isawig does not use running masses in the evaluation of higgsino-type couplings whereas Pythia does. This has been observed to lead to substantial differences between the widths calculated by the two programs (in rare cases factors of 2 or more).
- (2) $\alpha_{\rm s}$ at M_Z is used by Isawig in the calculation of the gluino decays. In the forthcoming update of Pythia where gluino decays are included, $\alpha_{\rm s}$ will be evaluated at the mass of the gluino.
- (3) Pythia and Herwig (Isasusy) do not use the same RGE's, so many parameters can differ quite substantially at the EW scale from the same GUT input, creating an "artificial" dissimilarity between the two programs. Ideally, one should compare models with identical EW scale mass spectra.

3 mSUGRA models

The models used in this study have not been chosen among the ones initially suggested in the ATLAS Physics TDR [3]. This is partly due to the exclusion of most of these points by LEP (essentially from bounds on the Higgs mass), and partly since it is interesting to enable a direct comparison between the capabilities of the LHC and other, future experiments. The 5 mSUGRA points shown in Table 1 have therefore been selected among 14 points which were defined by the CLIC physics study group [32]. More recently – too late to be included in the studies reported here – a new set of standard benchmarks points were proposed [2] which have now been adopted by both the CLIC and other linear collider communities. See [2] for mass spectra analogous to Table 1. To aid comparison, we briefly list the main differences/similarities between our points and the new benchmark points.

 $^{^{1}}$ This resulted in a few bug-fixes also in the Herwig code, so Isawig has had a few bugs in the ME calculation up to and including $\rm v.1104$

Table 1. Selected points of analysis in the mSUGRA parameter space, mass spectra as obtained with Isasusy, and total SUSY pair production cross section at the LHC

	P_2	P_7	P_9	P_{12}	F_2
	G	UT para	meters		
aneta	5	10	20	35	10
m_0	170	335	100	1000	2100
$m_{1/2}$	780	1300	300	700	600
$\operatorname{sign}(\mu)$	+	+	+	_	+
A_0	0	0	0	0	0
	N	lass spe	ctrum		
h^0	118	123	115	120	119
A^0, H^{\pm}, H^0	1100	1663	416	944	2125
$ ilde{\chi}_{1}^{0}$	325	554	118	293	239
$ ilde{\chi}^0_2, ilde{\chi}^+_1$	604	1025	217	543	331
$ ilde{\chi}^0_3$	947	1416	399	754	348
$\tilde{\chi}_4^0, \tilde{\chi}_2^+$	960	1425	416	767	502
$ ilde{g}$	1706	2752	707	1592	1442
$ ilde{e}_{ m R}, ilde{\mu}_{ m R}$	336	584	156	1031	2108
$ ilde{ au}_1$	334	574	126	916	2090
$ ilde{e}_{ m L}, ilde{\mu}_{ m L}$	546	917	231	1098	2126
$ ilde{ au}_2$	546	915	240	1051	2118
$ ilde{ u}$	541	913	217	1095	2125
$ ilde{q}_{ m R}$	1453	2333	612	1612	2328
$ ilde{b}_1$	1403	2262	566	1412	2010
$ ilde{t}_1$	1189	1948	471	1241	1592
$ ilde{q}_{ m L}$	1514	2425	633	1663	2343
$ ilde{b}_2$	1445	2312	615	1482	2310
$ ilde{t}_2$	1443	2286	648	1451	2018
	LI	IC Para	meters		
	P_2	P_7	P_9	P_{12}	F_2
$\sigma_{\rm SUSY}$ [fb]	130	3.9	24000	110	110
$\times 30 \mathrm{fb}^{-1}$	3900	114	720000	3300	3300

- (1) Point "A" is a (150 GeV) lighter version of P_2 . The total SUSY (pair production) cross section is approximately 4 times larger than for P_2 : $\sigma_{\rm A} \approx 4\sigma_{P_2}$.
- (2) Points "B", "C", "I", and particularly "G" are similar to P_9 ; $\sigma_{P_0} \approx 0.5\sigma_{\rm B} \approx 5\sigma_{\rm C} \approx 2\sigma_{\rm I} \approx 3.5\sigma_{\rm G}$.
- (3) Point "D" is dissimilar to all our points. It is closest to P_2 , but has a 500 GeV lighter gluino, and 400 GeV lighter squarks which increases the LHC cross section by an order of magnitude.
- (4) Point "E" is a lower-mass version of F_2 , point "F" a higher-mass version. $\sigma_{F_2} \approx 13\sigma_{\rm F} \approx 0.05\sigma_{\rm E}$.
- (5) Point "H" is similar to P_7 but slightly heavier, giving a total LHC cross section² $\sigma_{\rm H} \approx (1/4)\sigma_{P_7}$.

Table 2. Selected points of analysis in the $\lambda - \lambda'$ parameter space. The last column corresponds to the "natural coupling" scenario proposed in [23]. $\hat{m} \equiv m/v = m/126\,\mathrm{GeV}$ and $m_{q_j} \equiv (1/2)(m_{u_j} + m_{d_j})$. These models (column n) will be referred to as "nLLE", "nLQD", and "nLLE + nLQD" in the text below

			nodels
	a	b	n
		LLE	
λ_{ijk}	10^{-2}	10^{-4}	$\sqrt{\hat{m}_{e_i}\hat{m}_{e_j}\hat{m}_{e_k}}$
λ'_{ijk}	0	0	0
		LQD	
λ_{ijk}	0	0	0
λ'_{ijk}	10^{-2}	10^{-4}	$\sqrt{\hat{m}_{e_i}\hat{m}_{q_j}\hat{m}_{d_k}}$
]	LLE + LQD	
λ_{ijk}	10^{-2}	10^{-4}	$\sqrt{\hat{m}_{e_i}\hat{m}_{e_j}\hat{m}_{e_k}}$
$\lambda_{ijk} \\ \lambda'_{ijk}$	10^{-2}	10^{-4}	$\sqrt{\hat{m}_{e_i}\hat{m}_{q_j}\hat{m}_{d_k}}$

- (6) Point "J" is a high- $\tan \beta$ version of P_2 with very close to identical total cross section. The mass hierarchies are also very similar.
- (7) Point "K" is a large- $m_{1/2}$ sister of the only large- $\tan \beta$ model included in this work, P_{12} . The correspondingly larger masses yield a cross section $\sigma_{\rm K} \approx 0.04 \sigma_{P_{12}}$. The mass spectrum is similar to that of P_7 .
- (8) We have not included points at $\tan \beta = 45$, but point "M" can be seen as an even heavier version of point "K" $\approx P_{12}$ with a total cross section of only 0.1 femtobarns, and point "L" has a mass spectrum not greatly different from P_9 but with heavier squarks and gluinos giving a cross section an order of magnitude lower than for P_9 .

The total cross sections compared here include all MSSM pair production. Single sparticle production will give additional contributions depending on the strengths of the R-violating couplings.

One should keep in mind that all these points are defined for the MSSM, and as such have neutralino LSP's, a property which it has already been mentioned is not necessary in R-SUSY scenarios. Though we shall not do so here, it is certainly advisable to explore the experimental consequences of non-neutralino LSP's in more detail.

Both our points and the points in [2] assume a vanishing trilinear coupling at the GUT scale, i.e. $A_0=0$. In connection with this work, a small study of the direct consequences of that assumption upon the results presented here was performed. Varying A_0 between 0 and 500 GeV for P_2 , P_9 , and P_{12} gave only a weak variation $(\mathcal{O}(5\%))$ of the semi-inclusive L-violating branching ratios (e.g. $\mathrm{BR}(\tilde{\chi}^0_1 \to qq\nu)$), and so apart from the consequences of the distortion of the mass spectrum caused by $A_0 \neq 0$, the main signatures (number of leptons, number of jets, etc.) should be only mildly affected by changes to this parameter.

In addition to the mSUGRA parameters come the 9 λ (LLE) and the 27 λ' (LQD) couplings for which the scenarios listed in Table 2 have been studied for each mSUGRA

Point "H" gave a $\tilde{\tau}_1^+$ LSP when using the GUT input parameters in [2] with ISASUGRA. We therefore chose a 30 GeV larger value for m_0 , retrieving $\tilde{\chi}_1^0$ as the LSP

Table 3. Estimated trigger rates for background processes and trigger efficiency ranges for the various MSSM points and $I \hspace{-0.1cm}/\,$ -SUSY scenarios studied for $\mathcal{L}=3\times 10^{33}~\rm cm^{-2}s^{-1}$. The nomenclature follows the ATLAS standard, where e.g. "mu45I" means an isolated muon with $p_T>45~\rm GeV$, "me" stands for missing (transverse) energy, and "3j50" means 3 jets, each with $p_T>50~\rm GeV$. The total rate is smaller than the sum of the individual rates since there is a certain overlap, and the combined efficiencies can be larger than the individual efficiencies, since there is not a total overlap between the triggers

Trigger	Background rate	MSSM efficiency	LLE efficiency	LQD efficiency
mu45I + mu45I	$0.2\mathrm{Hz}$	1-5%	10-40%	1-10%
e45I + e45I	$0.1\mathrm{Hz}$	1-5%	135%	110%
mu15I + e15I	$0.1\mathrm{Hz}$	2–5%	20 – 60%	215%
mu40I + me75	$0.3\mathrm{Hz}$	1025%	40 - 75%	10 – 35%
e40I + me75	$0.2\mathrm{Hz}$	10 – 20%	15 - 70%	10 – 35%
j100 + mu40I	$0.5\mathrm{Hz}$	10 – 20%	45 - 70%	10 – 40%
j100 + e40I	$0.5\mathrm{Hz}$	515%	1565%	10 – 35%
j100 + me175	$0.3\mathrm{Hz}$	50 – 80%	3580%	2580%
3j50 + mu20I	$0.1\mathrm{Hz}$	5-15%	45 – 60%	12 – 40%
3j50 + e30I	$0.1\mathrm{Hz}$	5 - 10%	15 - 55%	10 – 35%
3j75+me125	$0.1\mathrm{Hz}$	3065%	3070%	40 – 90%
Total rate /combined efficier	2.1 Hz	60-90%	90-99.9%	60-96%

point. The reason we do not consider couplings larger than 10^{-2} is partly due to the present experimental bounds [33] and partly due to the fact that some implicit approximations in this analysis would break down for larger couplings:

- (1) the R couplings are not included in the RGE evolution of the SUSY parameters and
- (2) single sparticle production is not simulated. Note that the large-coupling (a) scenarios only observe the limits on individual couplings given in [33], not the limits on products of the couplings. Thus, these scenarios are useful for studying the consequences of having many large couplings, but one should keep in mind that they are unrealistic in that not all of the couplings can be simultaneously large.

On the other hand, if the R couplings get significantly smaller than 10^{-4} , the LSP lifetime can become so large that it decays outside the detector, mimicking the R-conserving scenarios which have already been extensively studied. For example, for the mSUGRA point F_2 , setting all λ couplings to 10^{-6} and all λ' couplings to zero results in a decay length for the LSP of $\tau c = 40 \,\mathrm{m}$. In the intermediate range, one may see the LSP decay directly inside the fiducial volume of the detector (see e.g. [34]), yet we abstain from relying on such a spectacular signature here so as not to be overly optimistic in our results.

4 Triggers for **///** -SUSY

A reasonable aim for the total L-SUSY dedicated trigger rate is about 1 Hz. We here focus on rates *after* the events have been filtered through the trigger system, i.e. we make

no distinction between trigger levels. This is a technical issue which requires more detailed knowledge of the detector performance at mid-luminosity than is currently parametrized in AtlFast. Specifically, no parametrization of the effects of pile-up at mid-luminosity is included, and so we here adopt a best-guess approach, performing the simulation without pile-up, and then multiplying the resulting trigger rates by a factor of 5/3 to estimate the true rates at $\mathcal{L}=3\times10^{33}\,\mathrm{cm^{-2}s^{-1}}$. This factor is based on the scaling exhibited by the inclusive electron, electron/photon, and E_T+2 -jets trigger rates presented in [3], Chapt. 11, from low to high luminosity.

To retain as much generality as possible in the trigger definitions, it is sensible to use the information contained in the $I\!\!\!L$ superpotential terms rather than a selection of decay modes to define the trigger menus. The λ (LLE) couplings are purely leptonic, and thus single sparticle production via these terms is not relevant for the LHC. Thus we are searching for at least two hard leptons (which, however, may be tauons), in most cases accompanied by E_T from escaping neutrinos. For the λ' (LQD) terms, we expect at least two leptonic objects accompanied by hard jets when the dominant production mechanism is MSSM pair production. Note that pure jet signatures would also be possible through single slepton production, $q_1\bar{q}_2 \to \tilde{\ell} \to q_3\bar{q}_4$. Single squark production via LQD requiries a lepton in the initial state and is thus suppressed at the LHC.

The triggers so far investigated are listed in Table 3, where background rates and efficiency ranges for all models investigated are shown. For comparison, results for MSSM scenarios are also given. The event generation was

Table 4. Numbers of generated events for the trigger study. The rates listed are total rates before trigger for $\mathcal{L} = 3 \times 10^{33} \, \mathrm{cm}^{-2} \mathrm{s}^{-1}$. QCD events with the p_{T} of the hard interaction below 1 GeV were not simulated

Event	rates and san	ple sizes	
Process	$\sigma \text{ [mb]}$	Rate [Hz]	$N_{ m gen}$
QCD $2 \to 2$			
$p_{\mathrm{T}} = 110\mathrm{GeV}$	55	1.6×10^{8}	2.5×10^{8}
$p_{\mathrm{T}} = 1075\mathrm{GeV}$	12	3.7×10^{7}	2.2×10^{8}
$p_{\mathrm{T}} = 75150\mathrm{GeV}$	5.5×10^{-3}	1.7×10^{4}	1.4×10^{7}
$p_{\rm T} > 150{\rm GeV}$	2.9×10^{-4}	8.7×10^{2}	1.1×10^{7}
$\overline{tar{t}}$	6.2×10^{-7}	1.9	5.9×10^{6}
Z/W	1.2×10^{-3}	3.6×10^{3}	1.8×10^{8}
ZZ/ZW/WW	1.2×10^{-7}	0.36	5.9×10^{6}

performed with an augmented version of Pythia 6.155 [35] and AtlFast v.2.53 [36]. With respect to AtlFast, an attempt was made at obtaining more believable muon and electron reconstruction efficiencies by including by hand a muon efficiency of 95% independent of muon momentum and an electron reconstruction efficiency of 80% for electrons with $p_{\rm T} > 50\,{\rm GeV}$ and 70% for electrons with $p_{\rm T} < 50\,{\rm GeV}$. These estimates are based on the ATLAS Physics TDR [3].

Background cross sections, pre-trigger event rates, and sample sizes are listed in Table 4. Though low- $p_{\rm T}$ QCD events have essentially no chance to pass triggers and much less the subsequent analysis cuts, the very high purities required for SUSY signal extraction do not immediately admit these events to be discounted entirely. Rather, a substantial sample of such events was generated with the object of placing an upper bound on the number of low- $p_{\rm T}$ QCD events remaining after cuts using Poisson statistics. This will be discussed in Sect. 5, however some cautiousness should be employed in interpreting the bounds obtained, since the Monte Carlo is here being stretched far into the tails of its $p_{\rm T}$ distributions.

We do not consider triple gauge boson production. The cross section (excluding Higgs-induced production) is around 100 fb [37], i.e. at the same level as interesting SUSY cross sections, yet invariant mass cuts on pairs of jets would presumably be able to reduce this background considerably, and so we do not believe that these processes are dangerous as background sources.

More detailed remarks and a large selection of plots of trigger rates and efficiencies versus thresholds can be found in [28].

From the efficiencies in Table 3, one easily sees how much cleaner the signatures of the purely leptonic (LLE) coupling are compared to the signatures involving quarks (LQD) where higher thresholds, due to the hadronic environment, mean smaller efficiencies. From this we conclude that it would be of interest to extend the LQD study, examining whether 2-jet triggers and/or 3-object triggers could enhance the efficiency.

Lastly, though the trigger proposals given here are designed explicitly with L-SUSY in mind, they show a certain overlap with triggers proposed for more conventional physics. The di-muon and 3-jets + lepton triggers, for example, have also been proposed for various Higgs searches. The di-electron trigger as well as 3-jets + electron are proposed to catch $t\bar{t}$ decays. Finally, the conventional SUSY searches also make use of multi-lepton, jets + L_T , and multi-jet signatures [38]. It is therefore not unlikely that the triggers proposed here can be incorporated to some extent into the conventional trigger programme.

5 Discovery of **I**-SUSY at the LHC

The main purpose here is to deliver an impression of what kind of signal strengths can be achieved at the LHC with $30\,\mathrm{fb^{-1}}$ integrated luminosity. To maintain generality in view of the more than thousand L-violating channels possible, we do not discuss invariant mass reconstruction or measurements of the SUSY parameters in general. We focus entirely on the isolation of candidate events through inclusive and kinematic event-shape variables in the attempt to obtain a statistically significant signal as compared with the background expectation after cuts. We do this for several models simultaneously (using neural networks in the final step), an approach which is complementary to the conventional one, where specific scenarios are studied one by one.

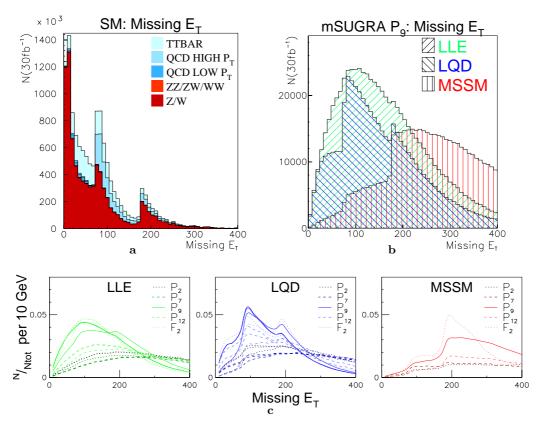
Note that no attempt is made, beyond a crude worstcase estimate, to include the effects of pile-up in this analysis.

5.1 Missing transverse energy

The post-trigger $\not\!E_T$ distribution for the SM and its composition is shown in Fig. 2a. Note that there are so few double gauge boson events that they are hardly visible on the plot. The peaks at $\not\!E_T = 75 \,\text{GeV}$ and at $\not\!E_T = 175$ are due to the me75 and me175 triggers becoming active.

In Fig. 2b the distributions for the most "low-mass" mSUGRA point, P_9 , are shown for $P_9(MSSM)$, $P_{9a}(LLE)$, and $P_{9a}(LQD)$. The degradation of the E_T signature in the E_T models is evident, though one observes by comparing with Fig. 2a that a cut at low E_T values is still possible. Note that the E_T trigger peaks mentioned above are absent for the LLE scenario; this simply because the LLE scenarios do not rely to so great an extent on the E_T triggers, cf. Table 3.

The full range of mSUGRA models are plotted in Fig. 2c. To enable the models to be shown on the same scale and to be distinguished from each other, the histograms have been normalized to unit area and smoothed. These plots are not intended to give detailed information, but rather to illustrate the spread between the models. Models with heavy squarks and gluinos $(P_7, F_2,$ and to some extent P_{12}) have rather flat, MSSM-like signatures whereas the models with lighter sparticles are peaked



at low E_T . This is an important point, since the light-sparticle scenarios have high production cross sections and the heavy-sparticle ones low cross sections. A cut on $E_T > 100 \,\text{GeV}$ seems a reasonable compromise between losing events in the peaked distributions (where we have many events anyway) and efficient background rejection required for the heavier scenarios (where we lose little by the cut but have fewer events).

5.2 Leptons and jets

Due to the fact that the LSP decays, one expects an increased number of leptons and/or jets in the $\not\!\!L$ -SUSY scenarios. In Figs. 3 and 4 the number of leptons is plotted versus the number of jets for each of the SM backgrounds and for $P_9(\text{MSSM})$, $P_{9a}(\text{LLE})$, and $P_{9a}(\text{LQD})$. All events satisfy $\not\!\!E_T > 100 \,\text{GeV}$.

The absolute normalizations are, of course, very different for each of the SM plots.

One notices that the number of reconstructed jets goes up to 15 on the plots in Figs. 3 and 4. The jet numbers are obtained using the AtlFast standard cone algorithm jet finder, employing a cone size of $\Delta R = ((\Delta \phi)^2 + (\Delta \eta)^2)^{1/2} = 0.4$ and with clusters up to pseudorapidities $|\eta| < 5$ included only if their transverse energies are above

 $E_T^{\rm min}=10\,{\rm GeV}$. Whether a resolution of up to 15 jets or more is possible (and reliable) in the finished experiment is questionable, yet the important point remains that there is more hadronic activity associated with the LQD scenarios than is the case for the MSSM, and we should be able to distinguish between the two possibilities using any jet finder.

The increased number of leptons in the LLE scenario as well as the increased number of jets (and a small increase in the number of leptons) in the LQD scenario relative to the MSSM are evident. Since the Z/W and high- $p_{\rm T}$ QCD backgrounds have the highest cross sections, a cut removing events in the lower left corner was performed, requiring $N_{\rm Jets}+N_\ell\geq 8$ or $N_\ell\geq 3$. This cut has a rejection factor of about 20 for the SM events and efficiencies above 75% for all $\not\!\!L$ -SUSY scenarios, again with a tradeoff between signal loss at low-mass points and efficient background rejection for high-mass points.

5.3 Additional variables

In addition to the above mentioned requirements, cuts on several other kinematical variables were performed before the neural network analysis below. We shall here only

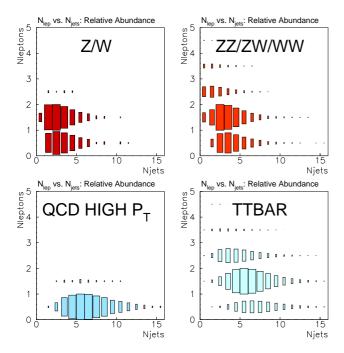


Fig. 3. Lepton versus jet multiplicity (see text) for background events surviving the cut on E_T . The numbering of the bins is such that the events with 0 jets are in the bin to the right of the number 0 and events with 0 leptons are in the bin above the number 0

briefly define and comment on these variables (see [28] for details):

- (1) The $p_{\rm T}$ of the hardest object (jet or lepton) in the event was required to be greater than 200 GeV.
- (2) We define the " $p_{\rm T}$ -weighted 4-object energy correlation" by

$$P_{4C} \equiv \frac{1}{12} \left(\frac{E_4}{E_3} + \frac{E_3}{E_2} + \frac{E_2}{E_1} \right) (p_{T1} + p_{T2} + p_{T3} + p_{T4}),$$
(2)

where E_1, \dots, E_4 (p_{T1}, \dots, p_{T4}) are the energies (transverse momenta) of the four hardest objects in the event. For pair-produced LSP's, one would expect four hard objects with more or less equal energies more often than would happen for background events. The energy fractions are weighted by the average $p_{\rm T}$ to give the variable some extra sensitivity against $t\bar{t}$ events. A cut at $P_{\rm 4C} > 200~{\rm GeV}$ was placed.

- (3) Events with Thrust greater than 0.85 were rejected. The Thrust calculation naturally suffers from the loss of particles down the beam-pipe at high pseudorapidities. Only particles with $|\eta| < 5$ are defined as being inside the active calorimetry range in AtlFast, and only these particles are included in the Thrust calculation.
- (4) Events with Oblateness greater than 0.4 were rejected³.
- (5) Events with Circularity less than 0.1 were rejected⁴.

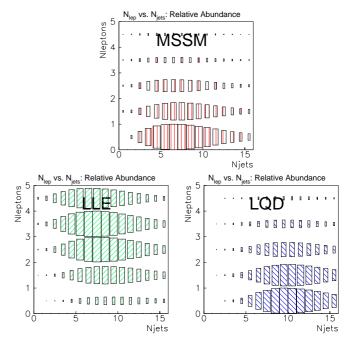


Fig. 4. Lepton versus jet multiplicity (see text) in mSUGRA P_9 for events surviving the cut on E_T . The numbering of the bins is such that the events with 0 jets are in the bin to the right of the number 0 and events with 0 leptons are in the bin above the number 0

5.4 Neural network cuts

It is clear that the above cuts do not define a dedicated search strategy. They were applied to all scenarios with no distinction between MSSM, LLE, and LQD models. A more comprehensive analysis would of course have to focus on each of these possibilities separately, and also some differentiation between the mSUGRA parameters would be required. In particular sparticles lighter than the top and ones heavier than the top could with advantage be searched for using separate strategies.

This highlights the fact that the mSUGRA parameter space, including now the \$\nsuperscript{L}\$ couplings, is not small. It was judged an uneconomical use of resources at this point to optimize a purely physics-based analysis for each of the many possibilities offered by this large parameter space. Instead, three neural networks were trained with post-trigger events to separate MSSM, LLE, and LQD scenarios, respectively, from the background distributions. Each network was thus trained not with one scenario but with equal numbers of events from 15 different scenarios with varying mSUGRA parameters and varying \$\nsuperscript{L}\$ coupling strengths, allowing the networks to pick out general qualities common to each class without overfitting to a particular model.

This procedure is certainly prone to the dangers which are always present when using neural networks on simulated data, in that the input parameters (*simulated* experimental observables) do not come with warning labels about where in their domains the simulated results can be trusted and where not. However, exercising caution on this

Note that Oblateness is calculated entirely in the transverse plane for hadron colliders

⁴ Same comment as for Oblateness

point, the method proposed here could be a useful alternative for exploring theories with large parameter spaces.

As inputs were used all of the above mentioned variables along with the $p_{\rm T}$ of the four hardest jets and the two hardest leptons. The networks employed were single-layer perceptrons using the gradient descent learning algorithm, with biased linear input and output neurons, and hidden neurons activated according to a biased sigmoid ("logistic") function. At the end of each learning period, the networks were trimmed using the OBD (optimal brain damage) prescription [39]. After ten such periods, the networks generally showed a negligible difference in performance on the learning sample as compared with the performance on an independent monitor sample, indicating that overfitting to the training samples is not a problem.

The training samples consisted of 3000 post-trigger SUSY events, selected equally among the appropriate scenarios, and 4000 background events, weighted according to their post-trigger cross sections to represent approximately 10^7 events in the learning algorithm. An output of zero (one) was the target for background (SUSY) events.

The finished LLE (LQD) network showed a clear preference for low-Thrust, multi-lepton (multi-jet), low-Oblateness events with a mixture of low and high E_T . For slightly higher Thrust values, low lepton momenta were preferred in the LLE case. For the LQD network, the most noteworthy additional feature was a strong relaxation of all other considerations for very high jet energies. Note that the background levels at low Thrust values suffer from some theoretical uncertainty due to the fact that parton showers have been used to generate the multi-jet final states, an approach which in the past has been known to give too few multi-jet events. Though it is not clear that present generators suffer from the same problems, it is important to note that there is a non-negligible and potentially dangerous uncertainty in any analysis relying on parton-shower simulations for large jet numbers and low Thrust values.

Processing now the full event samples remaining after the cuts described above through each of the three (MSSM, LLE, and LQD) networks, a final cut was made requiring outputs larger than 0.9. Since the learning samples were small compared to the full event samples (e.g. about 100,000 SUSY events were generated per scenario and only a few hundred used for training) no effort was made to exclude those events which had participated in the learning process from the analysis. This is, in principle, a source of error, yet we permit ourselves to ignore it due to the smallness of the learning samples and since any problems related to over-fitting have been minimized by OBD. For the SM backgrounds, the generated event samples had been depleted considerably by the initial cuts, and only the $t\bar{t}$ and double gauge boson samples had any events remaining at all after the network cuts (note that the learning samples used for training – for both background and SUSY – were post-trigger events).

The procedure used to construct upper bounds on the actual event numbers was, for N events remaining in a sample, to calculate the mean, μ , of the Poisson distri-

bution which has exactly 5% chance to result in N or fewer events. μ is then interpreted as a "95% CL" upper bound on the number of events which could have passed the cut. For the low- $p_{\rm T}$ QCD events, this number was then subjected to the same rejection factors under cuts as the high- $p_{\rm T}$ sample (later the rejections for the $t\bar{t}$ sample were used for both), and the double gauge boson rejection factors were used for the upper bound on single gauge events.

Typically, for $30 \,\mathrm{fb^{-1}}$, between 500 and 1000 signal events remain after cuts for P_2 , P_{12} , and F_2 . Many more of course remain for P_9 because of the larger cross section, but there is no hope for P_7 with only 114 events expected in total in $30 \,\mathrm{fb^{-1}}$ of data. Yet one should bear in mind that single sparticle production which has not been included here could significantly increase the cross section if the R couplings are not much smaller than the gauge couplings. For a hadron machine like the LHC, this effect would only be large for the LQD terms since single slepton resonances would then be possible. Of course, if R terms are present, single squark production would be possible as well

5.5 Results

We define the statistical significance with which a discovery can be made by

$$P = \frac{S}{\sqrt{S+B}} \tag{3}$$

and conservatively interpret P>5 rather than the conventional $S/(B^{1/2})>5$ to mean that a 5σ discovery will be possible. Using the event numbers obtained in the analysis (the estimates on B being 95% CL upper bounds) results in the P values listed in Table 5.

In reality, P depends on (unknown) systematic QCD uncertainties (parton distributions etc) and should be corrected for the effects of pile-up, and so we can only be confident that a 5σ discovery is possible if P is somewhat larger than 5. Therefore, aside from working with the definition, (3), we attempt to define a more pessimistic quantity in a very crude, ad hoc manner which we shall call $P_{\rm corr}$.

The non-inclusion of pile-up results in too optimistic estimates of S/B. To include an estimate of the reduction of this ratio, we rewrite (3) to

$$P = \frac{\sqrt{S}}{\sqrt{1 + B/S}},\tag{4}$$

where we now include the effects of pile-up by multiplying B/S by some factor. That twice as many background events per signal event could be passing the analysis if pile-up was included seems a reasonably pessimistic guess.

Furthermore, assuming that the intrinsic uncertainty on both S and B coming from uncertainties on QCD parameters will, to a first approximation, work in the same direction and with a comparable magnitude for both B and S, we expect that the denominator in the above formula is not affected by this uncertainty, and so we include

Table 5. ATLAS discovery potential and corrected discovery potential (see text) for all SUSY scenarios investigated using each of the three networks. The numbers shown correspond to an integrated luminosity of $30\,\mathrm{fb}^{-1}$

		Network	
JSY	MSSM	LLE	LQD
oint	$P/P_{\rm corr}$	$P/P_{\rm corr}$	$P/P_{\rm corr}$
LLE $2a$	24.3/16.2	25.5/17.1	25.4/17.1
LLE 2b	24.5/16.3	25.8/17.3	25.7/17.3
LLE $2n$	23.2/15.4	24.7/16.5	24.3/16.3
$^{LE}_{a}$	0.7/0.4	0.7/0.4	0.8/0.5
LLE b	0.8/0.4	0.8/0.4	0.8/0.5
n	0.7/0.4	0.7/0.4	0.8/0.5
LLE a	191/153	315/256	218/176
LLE)b	190/153	316/256	218/176
LLE n	166/133	257/208	169/135
2a	23.4/15.5	25.6/17.2	25.5/17.2
$_{2b}^{LE}$	23.4/15.5	25.5/17.2	25.5/17.2
2n	21.8/14.4	24.2/16.2	24.3/16.3
LLE $2a$	11.3/7.0	14.0/8.8	13.3/8.4
LLE 2b	11.2/6.9	13.7/8.7	13.1/8.2
$^{LE}_{2n}$	9.9/6.1	12.4/7.8	12.3/7.7
LQD	20.9/13.7	24.3/16.2	24.8/16.6
LQD 2b	21.4/14.1	24.7/16.5	25.3/17.0
LQD 2n	21.5/14.1	23.3/15.5	24.2/16.2
LQD 'a	1.0/0.6	1.0/0.6	1.1/0.6
LQD 'b	1.0/0.6	1.0/0.6	1.1/0.7
LQD 'n	1.0/0.6	1.0/0.6	1.1/0.6
LQD	116/91.6	153/122	125/99.0
_QD	113/88.7	151/121	123/97.6
LQD On	113/88.5	131/104	110/86.6
$\frac{QD}{2a}$	15.7/10.0	19.2/12.5	20.9/13.7
QD .2b	15.8/10.1	19.4/12.6	21.1/13.9
$_{2n}^{QD}$	16.6/10.6	18.6/12.1	20.9/13.8
QD	7.0/4.2	9.5/5.9	10.5/6.5
_QD	7.0/4.2	9.4/5.8	10.5/6.5
LQD $2n$	6.9/4.2	8.8/5.4	10.3/6.4

the QCD-related uncertainties by reducing the number of signal events in the numerator by a factor of 1.5, believing this to be an adequate worst-case estimate. This yields the following form for the "corrected discovery potential":

$$P_{\rm corr} = \frac{S}{\sqrt{1.5S + 3B}}. ag{5}$$

Of course, this quantity should not be taken too seriously. We list it in Table 5 merely to show the effects of the stated factors on the discovery potential, i.e. a reduction of S/B by a factor of 2 combined with a reduction of both S and B by 2/3.

With regard to the sensitivity of this analysis on systematic uncertainties on the normalization of B, note that

only for P_9 do we have an $S/B \gg 1$. For the P_2 , P_{12} , and F_2 scenarios S/B lies between one half and unity. We do not estimate this to be a serious problem since our background estimate is only a 95% CL upper limit (larger event samples would most likely bring the high- p_T QCD component down) and since the background normalization can presumably be determined to better than a factor 2 (as is used in $P_{\rm corr}$) using complementary regions of phase space where the SUSY population is low or vanishing.

What one can see in Table 5 is again that the LLE scenarios typically yield much purer event samples than the LQD ones, due to the hadronic environment at the LHC. It is also worth noticing that it is not easy, from this analysis alone, to discriminate between MSSM, LLE, and LQD scenarios. This is due to the fact that the three networks were trained independently, i.e. they were taught to reject SM events but not events from the other scenario types.

A suggestion for how we might have gained further insight would be to construct *one* network with one output node for each class of models, requiring an output of $(0,0,\cdots)$ for background events, $(1,0,0,\cdots)$ for events of class 1, $(0,1,0,0,\cdots)$ for events of class 2, and so on. One would then be able to construct a measure for the relative probability of the events surviving cuts belonging to a given class of models, by comparing their n-dimensional distribution in the network output space with the expected background distribution.

6 Outlook and conclusion

6.1 Outlook

Though some preliminary studies have been performed in the present work, the field is large and many important tasks remain. Recently, a significant theoretical effort has been dedicated to studying the case of baryon number violation [40–42]. Both single sparticle production and baryon number violating SUSY will be included in the Pythia generator in the foreseeable future.

This will hopefully spur more LHC activity, with comprehensive studies of both lepton and baryon number violating scenarios. Preliminary studies indicate a lessening of the reach of the LHC in baryon number violating scenarios [40], and it would be of interest to explore this reach with the full range of production and decay mechanisms included. In addition, studies should certainly be carried out for mSUGRA benchmark points without neutralino LSP's.

Finally, triggers dedicated for R-SUSY should be incorporated in the standard ATLAS trigger programme.

6.2 Conclusion

1278 decay modes of supersymmetric particles into standard model particles through lepton number violating couplings have been implemented in the Pythia event generator. Combining this augmented version of the generator

with a crude simulation of the ATLAS detector, trigger menus for mid-luminosity running of the LHC have been proposed and seen to have a high acceptance of supersymmetric events in several L-violating supergravity scenarios while still giving event rates in the 1 Hz region.

Taking these trigger menus as basis, the possibility for a 5σ discovery after $30\,\mathrm{fb^{-1}}$ data taking was estimated for each investigated model, using a technique based on simultaneous classification of groups of models rather than detailed studies of single models.

For cross sections down to 10^{-10} mb (or, roughly, for points with $m_0 < 2$ TeV and $m_{1/2} < 1$ TeV) it was found that a 5σ discovery was possible for all scenarios with $30 \, \mathrm{fb^{-1}}$ of data. It is estimated that uncertainties related to QCD parameters or pile-up in the detector, both of which have not been taken into account in the present analysis, could not significantly affect this conclusion.

L-violating decays of the gluino and the possibility of invoking B-violation will be implemented in the Pythia generator within a foreseeable future.

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